

Data Path Queries over Embedded Graph Databases

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VardiFest'22, Haifa, Israel

Thank you, Moshe!!

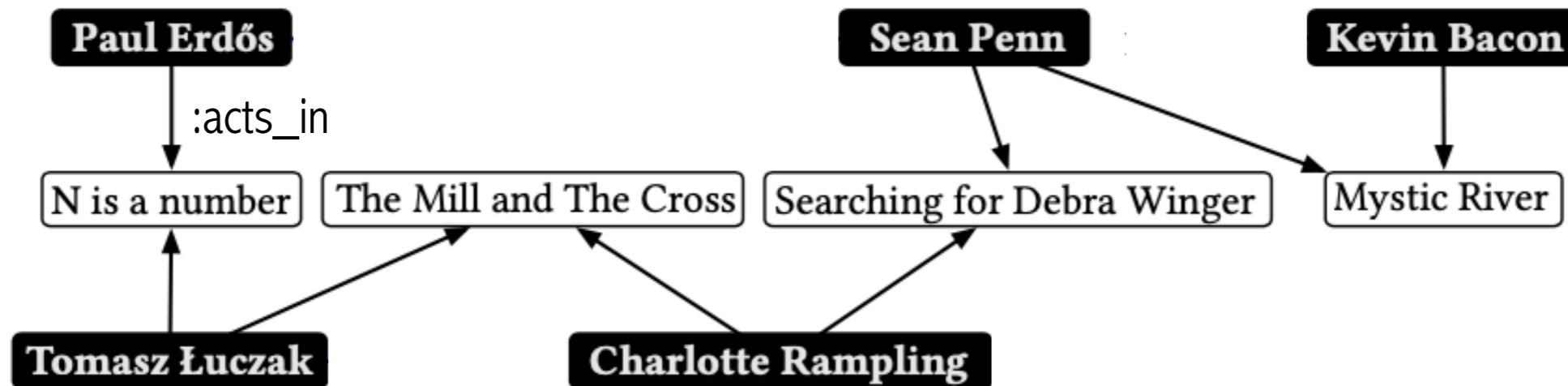
This talk is in honor of Moshe's fundamental contributions in diverse fields especially:

- Database theory (in particular, over graph databases)
- Finite Model Theory
- Automata and Logic
- Boolean satisfiability

The presented result was a modest attempt to learn from Moshe's diversity; it aimed to connect graph databases and SMT

Graph DB: Classic Setting

Output actors that have a finite Bacon number in a movie DB



Regular Path Query (RPQ):

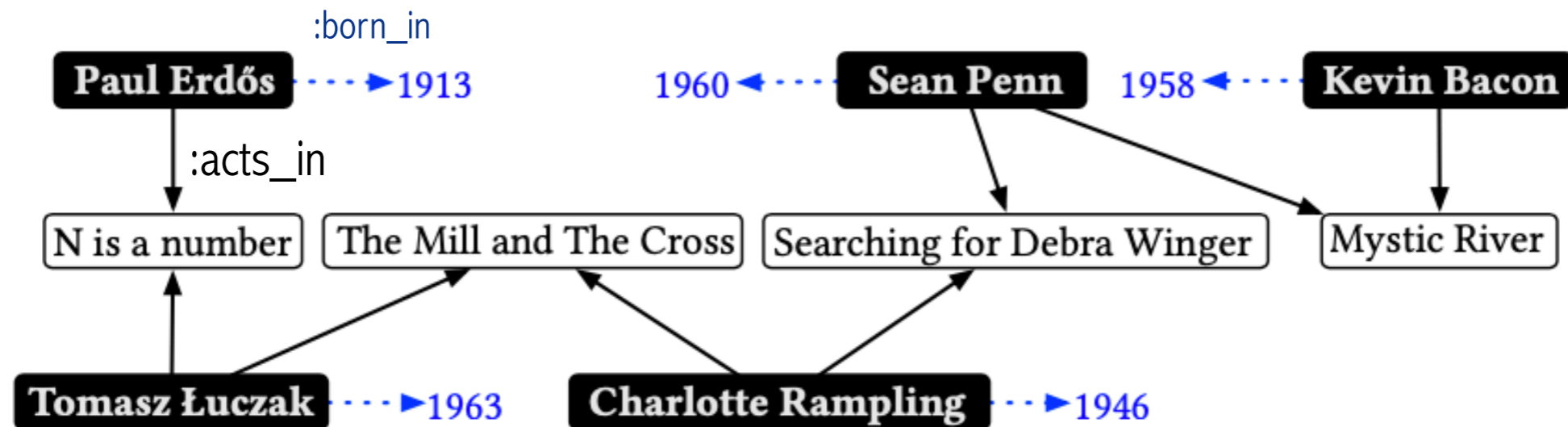
$x \longrightarrow_L \text{Bacon}$, where $L = (:\text{acts_in} + :\text{acts_in}^{-1})^*$

Desirable data complexity (query L fixed):

NLogspace

„Data“ Querying

Output actors that have a finite Bacon number in a movie DB,
whose age is at least 30 years apart from Bacon



Data Queries can get complicated:

1. String data type: similar names along path (small edit distance)
2. Non-linear arithmetics: „nearby“ cities along path (Euclidean distance)

Regular Data Path Queries (RDPQ)

(Libkin, Martens, Vrgoc [early 2010s])

Key idea: data words, register automata (Kaminski&Francez)

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over $\{\text{acts_in}, \text{acts_in}^{-1}\}$

$\cup \mathbb{Z}$



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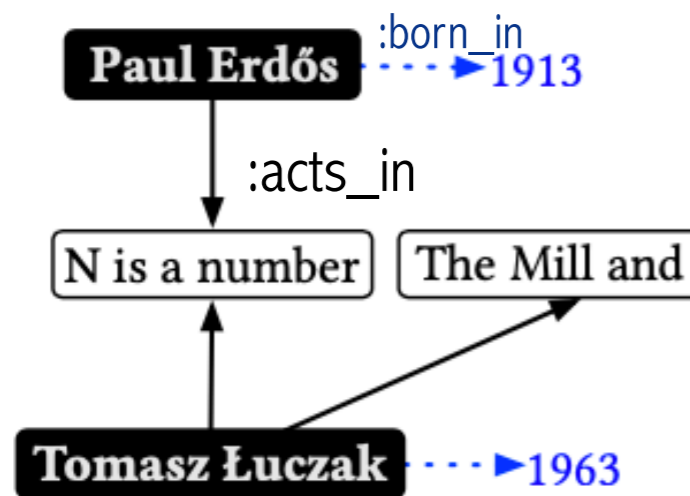
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$(1913)(\text{acts_in})(\text{acts_in}^{-1})(1963)$



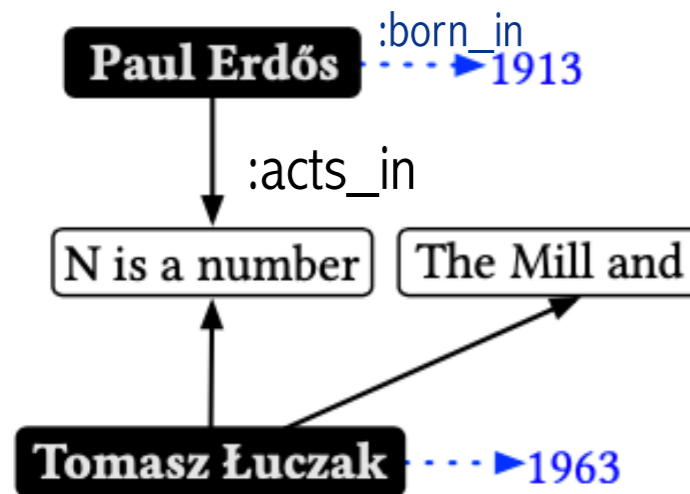
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Bacon \longrightarrow_L *Person*, where

$$L = x \downarrow (:\text{acts_in} + : \text{acts_in}^{-1})^* x^=$$

Gets actors *of equal age*

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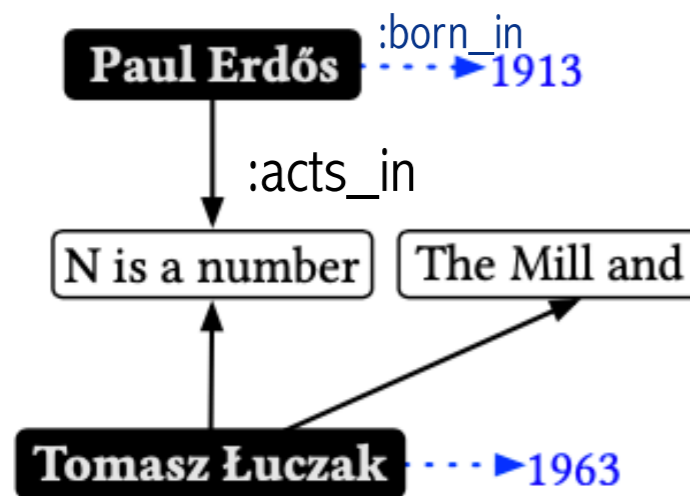
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Theorem: RD PQ with register automata has NL data complexity.

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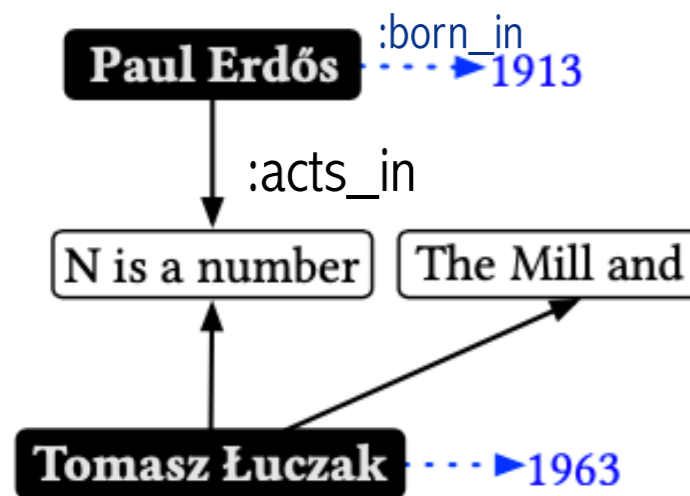
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Gets actors of equal age

Theorem: RDPQ with register automata has NL data complexity.

No domain-specific reasoning (e.g. no arithmetics)

Our Main Result

NLogspace data complexity for RDPQ with:

1. Domain-Specific Reasoning (over integer linear arithmetic, theory real closed fields, and various string theories)
2. Generic data graph model

Key ideas:

1. Embedded Finite Model Theory
2. Theory-Aware Register Automata

Our Main Result

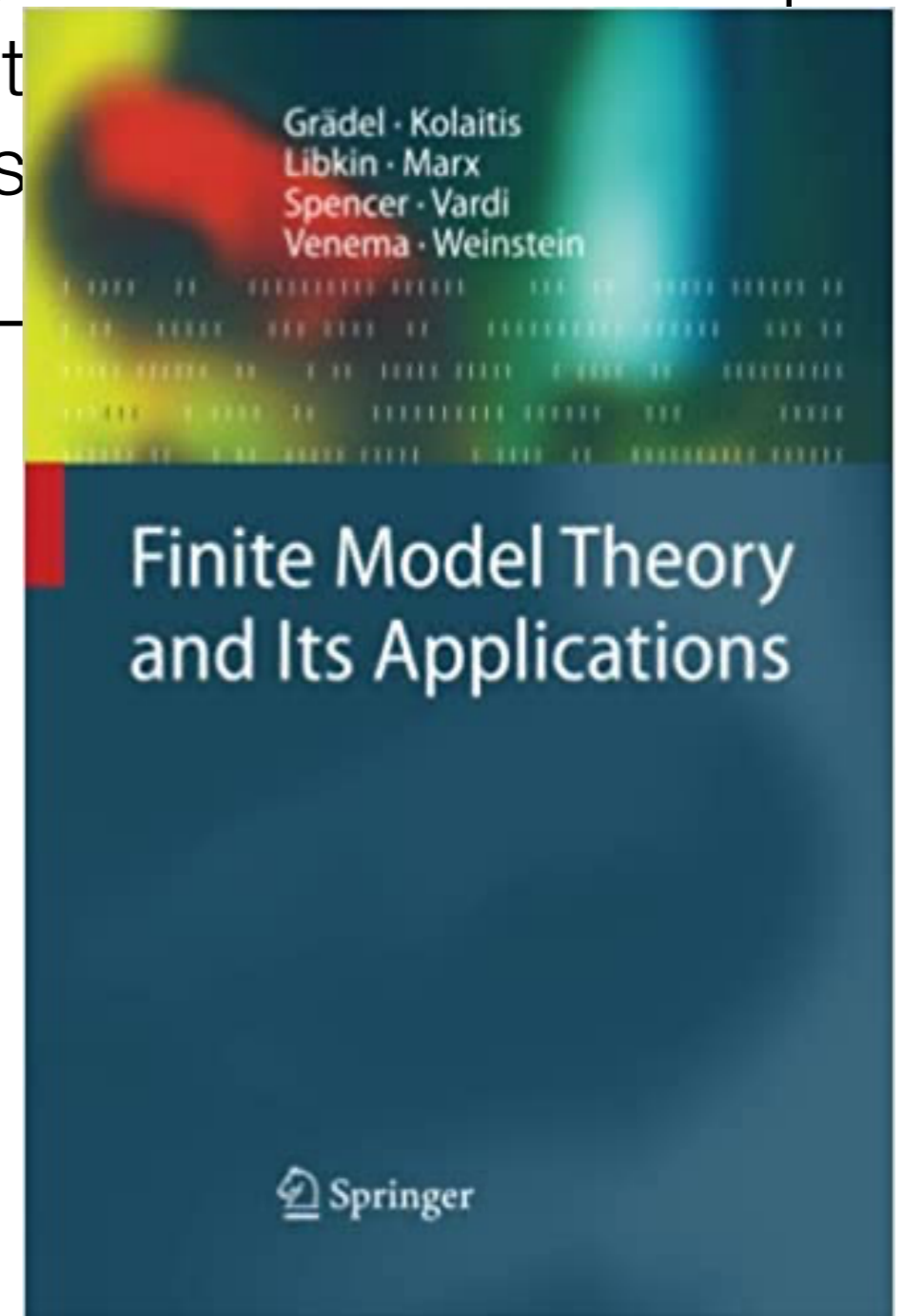
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1. Embedded Finite Model Theory

2. Theory-Aware Register Automata



Key Idea #2: „Theory-Aware“ Register Automata

First approach:

- (1) fix an infinite structure \mathcal{S} with a decidable theory
- (2) Registers take values and permit operations from \mathcal{S}

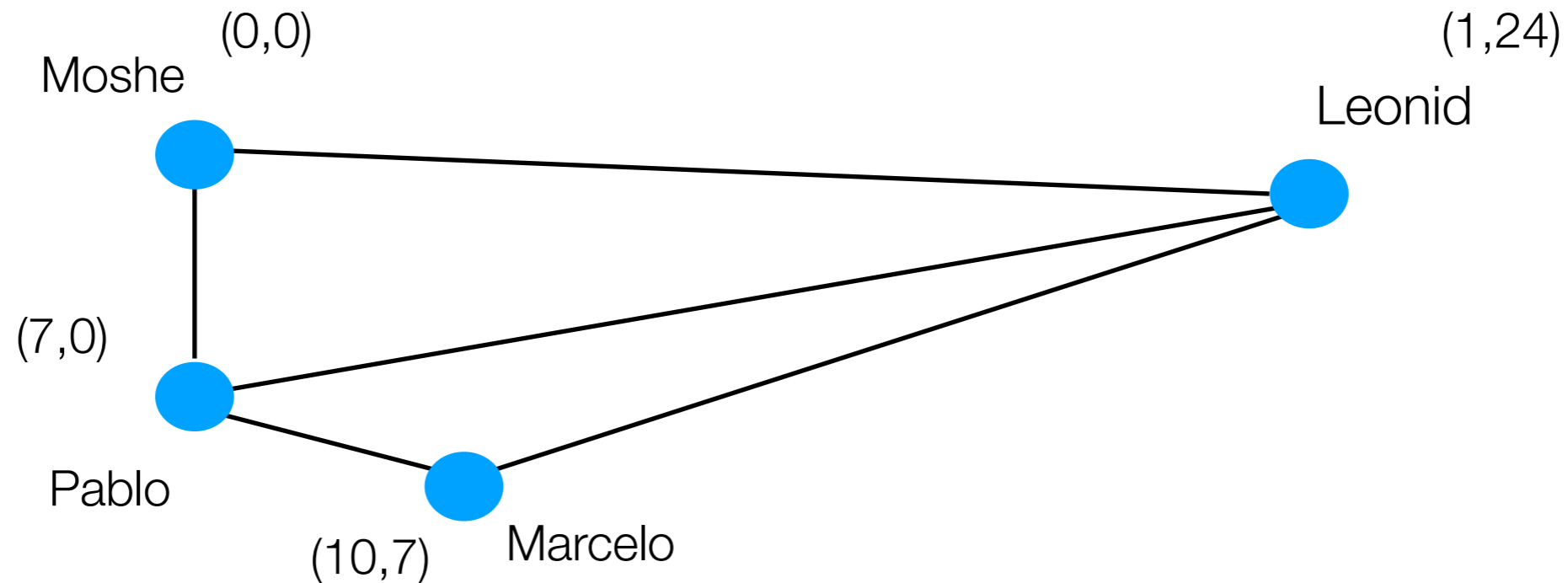
Problem: undecidable emptiness already for $\mathcal{S} = \langle \mathbb{N}; +, 1, = \rangle$

Our solution:

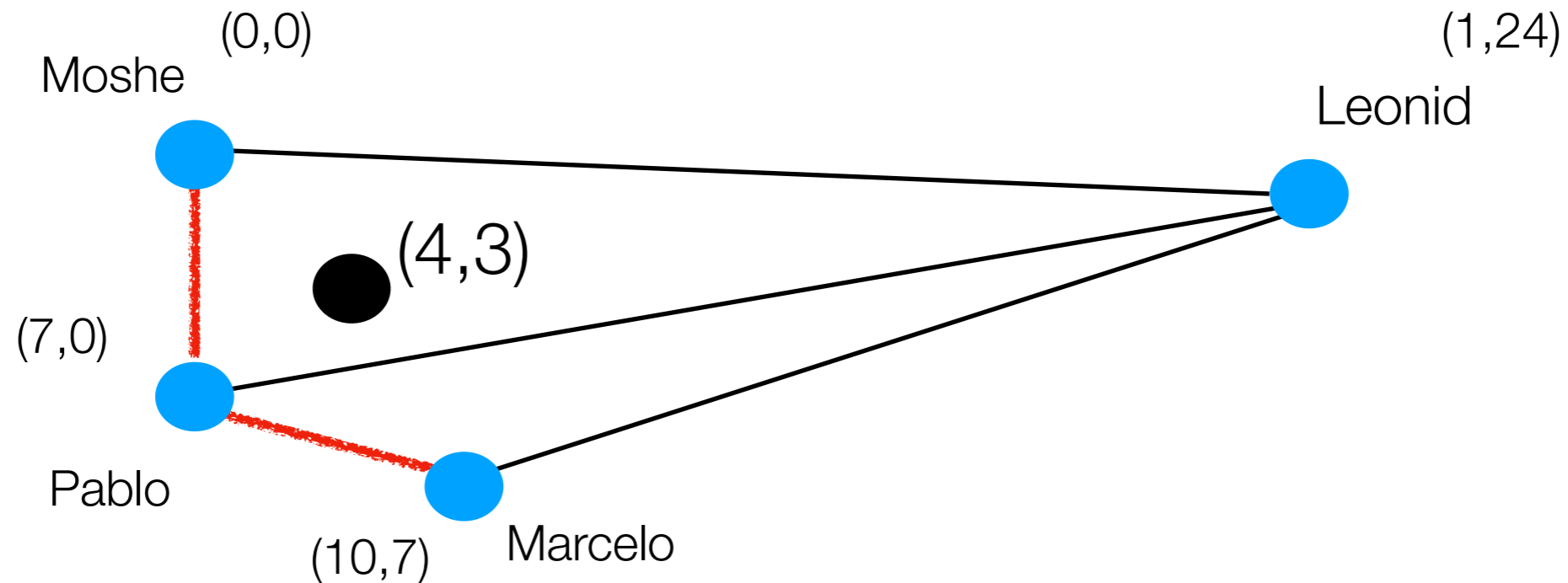
- (1) Distinguish between active-domain and general-valued registers
- (2) General-valued registers are bounded-rewrite
- (3) First-order guards

For important theories T (over integers, reals, and strings), we show that T -RD PQ querying still has NL data complexity!

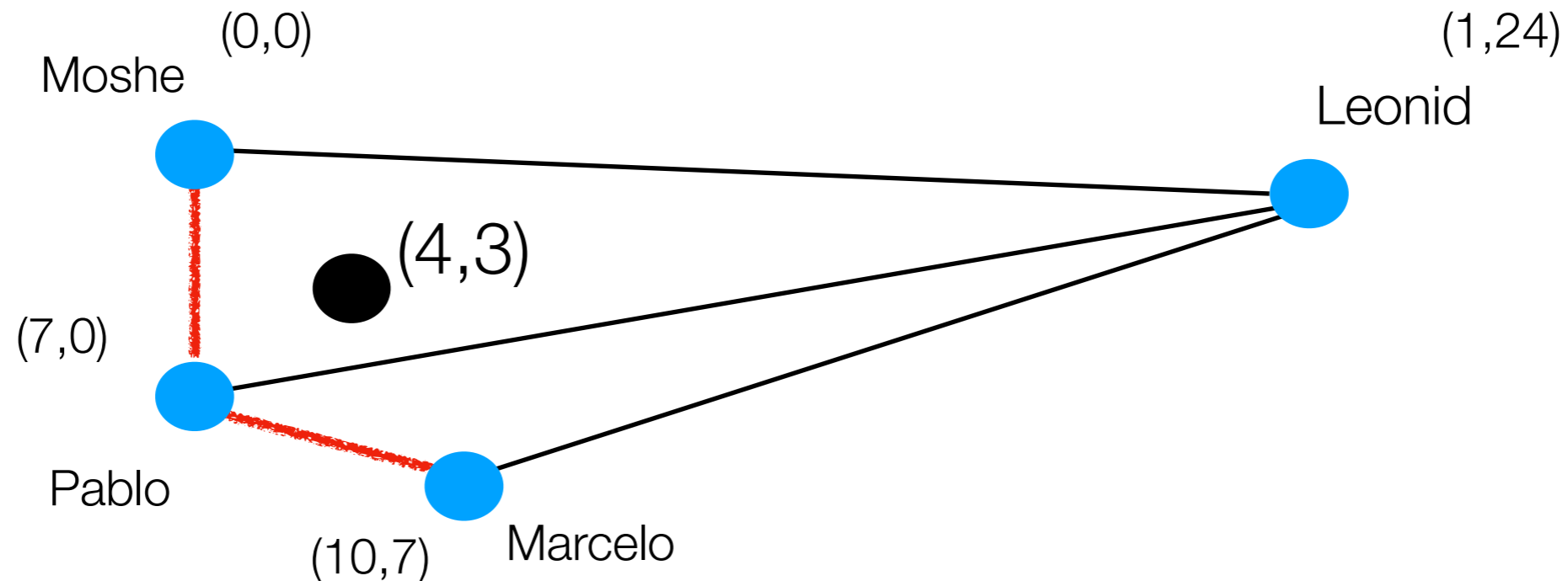
Ex: Path of Coauthors whose „center“ is of distance ≤ 6



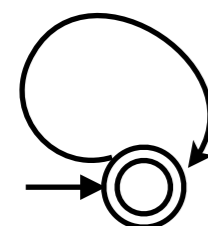
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Two unrestricted registers: r_1, r_2



$$\text{coauthors}(curr, next) \wedge \exists x, y \in \text{adom} \left(x\text{val}(curr, x) \wedge y\text{val}(curr, y) \wedge \sqrt{(x - r_1)^2 + (y - r_2)^2} \leq 6 \right)$$

Theorem (formally)

Theorem:

- RDPQ with $\langle \mathbb{Z}; +, <, 1, 0 \rangle$ -RA is NL-complete
- RDPQ with $\langle \mathbb{R}; +, \times, <, 1, 0 \rangle$ -RA is NL-complete
- RDPQ with RA over existential positive string equation is NL-complete
- RDPQ with RA over existential automatic structures is NP-hard, but is NL-complete under log-size hypothesis.

Key Technique

Restricted Register Collapse: linear arithmetic, real closed fields

Each unrestricted register could be effectively replaced by active-domain registers

Extends the classic notion of Restricted Quantifier Collapse from EFMT

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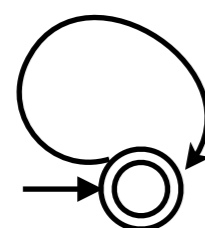
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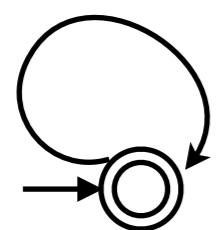
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To remove r_2 , we can rewrite this to an expression in terms of roots of $(x - r_1)^2 + (y - r_2)^2 \leq 36$ treated as univariate r_2 -polynomial, for some active-domain values x, y

Future Work

- Query containment for RDPQ and extensions
- NL data complexity for a more expressive query language, e.g., Regular Data Queries (RDQ)?

Thanks!